### Robust Single-Qubit Process Calibration via Robust Phase Estimation

#### Shelby Kimmel, Guang Hao Low, Ted Yoder

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JOINT CENTER FOR QUANTUM INFORMATION AND COMPUTER SCIENCE



### Imagine...



#### Imagine...





[Monroe Lab]

### Imagine...





[Monroe Lab]

- All gates need to be tuned
- State preparation is off
- Measurements are off

Want to quickly determine imperfections in gate controls and then tune to fix.

#### Need to Calibrate Operations



Ideal Unitary U

#### Need to Calibrate Operations



#### Need to Calibrate Operations





Ad hoc Rabi – Ramsey Sequences.



**Process Tomography** 



**Process Tomography** 

- Need perfect state preparation and measurement
- Need perfect additional gates
- Time consuming: need to learn 12 parameters to extract  $\phi$  and  $\epsilon$





#### **Randomized Benchmarking**





#### Randomized Benchmarking

- Don't need perfect state preparation and measurement
- Must be able to perform single-qubit Cliffords (although not perfectly)
- Time consuming: need to learn 9 parameters to extract  $\phi$  and  $\epsilon$







#### **Robust Phase Estimation**

- Don't need perfect state preparation and measurement
- No additional gates, except Z-rotations
- Learn  $\phi$  and  $\epsilon$  with optimal efficiency
- Non-adaptive
- Accommodates additional errors like depolarizing noise.

### Outline

- Motivation for Robust Phase Estimation
- Robust phase estimation
- Application to Calibration



Can sample from 2 binomial random variables with probability of "heads"

$$\frac{1+\sin k\theta}{2}, \qquad \frac{1+\cos k\theta}{2}$$

For k in  $\mathbb{Z}$ , each in time k



Can estimate  $\theta$  with standard deviation  $\sigma(\theta) \sim \frac{1}{\sqrt{T}}$ 



$$\frac{1 + \sin k\theta}{2}, \qquad \frac{1 + \cos k\theta}{2}$$
  
For k in Z, each in time k

$$k = 1$$



$$\frac{1 + \sin k\theta}{2}, \qquad \frac{1 + \cos k\theta}{2}$$
For k in Z, each in time k
$$k = 1 \qquad k = 2$$



$$\frac{1 + \sin k\theta}{2}, \qquad \frac{1 + \cos k\theta}{2}$$
For k in Z, each in time k
$$k = 1 \qquad k = 2 \qquad k = 4$$



Can estimate  $\theta$  with standard deviation  $\sigma(\theta) \sim \frac{1}{T}$ Optimal – by information theory.





$$\frac{1+\sin\theta}{2} + \delta_{k1}, \qquad \frac{1+\cos\theta}{2} + \delta_{k2}$$
  
Using only  $k = 1$  can't get an accurate estimate!







Can estimate  $\theta$  with standard deviation  $\sigma(\theta) \sim \frac{1}{T}$ , as long as  $|\delta_k| < .35$  for all k.

Want 2-outcome experiments with probabilities like:



Want 2-outcome experiments with probabilities:



 $A = \pi(1 + \epsilon)$  is total amplitude of rotation

Want 2-outcome experiments with probabilities:



rotation

Want 2-outcome experiments with probabilities:



Don't have perfect state prep and measurement? OK! Just add to  $\delta$  error.

Want 2-outcome experiments with probabilities:



Have depolarizing errors? OK! Just add to  $\delta$  errors.

Want 2-outcome experiments with probabilities:



Heisenberg limited! Estimate of  $\epsilon$  with standard deviation  $\sigma(\epsilon) \sim \frac{1}{N}$ , where N is the number of times  $\widetilde{U}$  is applied.

Want 2-outcome experiments with probabilities:



Heisenberg limited! Estimate of  $\phi$  with standard deviation  $\sigma(\phi) \sim \frac{1}{N}$ , where N is the number of times  $\widetilde{U}$  is applied.



- Don't need perfect state preparation and measurement
- No additional gates, except Z-rotations
- Learn  $\phi$  and  $\epsilon$  with optimal efficiency
- Non-adaptive
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#### **Open Questions**

- Multi-Qubit Operations?
- No perfect Z-rotation?
- Connection to Randomized Benchmarking

### Think this might be useful?





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